

LINEAR PROGRAMMING PROBLEM—GRAPHICAL SOLUTION AND EXTENSION

MULTIPLE CHOICE QUESTIONS

- Which of the following is not correct ?
 - The graphic approach to an LPP is most suitable when there are only two decision variables.
 - A possible solution on the graph corresponds to every point (x, y) .
 - ☒ The graphic approach to an LPP is applicable when the number of decision variables are more than the number of constraints.
 - The common region that satisfies all the constraints is called the feasible (convex) region.
- A feasible solution to an LPP
 - ☒ must satisfy all of the problem's constraints simultaneously.
 - must be a corner point of the feasible region.
 - need not satisfy all of the constraints, only some of them.
 - must optimize the value of the objective function.
- Which of the following is not correct ?
 - The graphic approach to the solution of LPP's cannot handle problems with more than three variables.
 - ☒ A feasible solution to an LPP is one that satisfies at least one of the constraints of the problem.
 - An optimum solution to an LPP is a feasible solution which optimizes the objective function.
 - ☒ The feasible region is also termed as the solution space.
- Which of the following is not correct ?
 - Feasible solution of an LPP is independent of the objective function.
 - The feasible region of an LPP must be a convex set.
 - The feasible region for a constraint is restricted if its ' $\geq$ ' or ' $\leq$ ' sign is replaced by a '=' sign.
 - ☒ It is not possible to obtain feasible solution of an LPP by graphical method.
- An iso-profit line represents
 - ☒ an infinite number of solutions all of which yield the same profit.
 - an infinite number of optimum solutions.
 - an infinite number of solutions all of which yield the same cost.
 - a boundary of the feasible region.
- If an iso-profit line yielding the optimum solution coincides with a constraint line, then
 - the solution is unbounded.
 - the solution is infeasible.
 - the constraint which coincides is redundant.
 - ☒ none of the above.
- If two constraints do not intersect in the positive quadrant of the graph, then
 - one of the constraint is redundant.
 - ☒ the solution is infeasible.
 - the solution is unbounded.
 - none of these.
- Which of the following is not correct ?
 - An infeasible solution exists, when there is no feasible solution.
 - Iso-profit lines on a graph of an LPP would always be parallel to each other.
 - ☒ An iso-cost line cannot be parallel to the line of any constraint.
 - Every LPP has a unique optimum solution.
- Using graphic method, the optimum solution of the LPP of maximizing $z = 10x + 15y$ subject to $2x + y \leq 26$, $x + 2y \leq 28$, $y - x \leq 5$ and $x \geq 0$, $y \geq 0$ is obtained as
 - ☒ $x = 8$ and $y = 10$.
 - $x = 6$ and $y = 1$.
 - $x = 6$ and $y = 10$.
 - $x = 8$ and $y = 8$.
- Given an LPP to maximize $z = -5x_2$ subject to $x_1 + x_2 \leq 1$, $0.5x_1 + 5x_2 \geq 0$, and $x_1 \geq 0$, $x_2 \geq 0$. Using graphical method, we have
 - no feasible solution.
 - unbounded solution.
 - unique optimum solution.
 - multiple optimum solutions.

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OPERATIONS RESEARCH

11. Which of the following is not correct ?
- (a) An LPP with an unbounded feasible region would obviously have unbounded solution.
 - ~~(b)~~ For an LPP, the feasible region may change if non-binding constraints are deleted.
 - (c) A redundant constraint represents an abundant resource.
 - (d) It is possible for the objective function value of an LPP to be the same at two distinct extreme points.
12. The general linear programming problem is in standard form, if
- ~~(a)~~ the constraints are strict equations.
 - ~~(b)~~ the constraints are inequalities of ' $\leq$ ' type.
 - (c) the constraints are inequalities of ' $\geq$ ' type.
 - (d) the decision variables are unrestricted in sign.
13. Which of the following is not correct ?
- (a) Graphical method of linear programming is not useful when there are only two decision variables.
 - (b) Solution of a maximization LPP when permitted to be infinitely large is called unbounded.
 - ~~(c)~~ Optimum solution to an LPP always lies at least on the two vertices of the feasible region.
 - (d) It is possible for the objective function value of an LPP to be the same at two distinct extreme points.
14. Which of the following statements is wrong ?
- (a) Slack variables are used to convert the inequalities of the type ' $\leq$ ' into equations.
 - (b) Surplus variables are used to convert the inequalities of the type ' $\geq$ ' into equations.
 - ~~(c)~~ An LPP with all its constraints are of the type ' $\geq$ ' is said to be in *standard form*.
 - (d) An LPP with all its constraints are of the type ' $\leq$ ' is said to be in *canonical form*.

ANSWERS

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|---------|---------|---------|----------|---------|
| 1. (c) | 2. (a) | 3. (b) | 4. (d) | 5. (a) |
| 6. (d) | 7. (b) | 8. (c) | 9. (a) | 10. (a) |
| 11. (b) | 12. (a) | 13. (c) | 14. (c). | |

REVIEW QUESTIONS

1. What are the essential characteristics of a linear programming model?

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MULTIPLE CHOICE QUESTIONS

- Given a system of m simultaneous linear equations in n unknowns ($m < n$), the number of basic variables will be
 - ☒ (a) m ,
 - (b) n ,
 - (c) $n - m$,
 - (d) $n + m$.
- Which of the following is not correct?
 - (a) The general LPP with m constraints in n unknowns ($m < n$) gives $\binom{n}{m}$ basic solutions.
 - (b) A basic solution that satisfies all the constraints and non-negative restrictions is called a basic feasible solution.
 - (c) A basic solution in which at least one basic variable vanishes is zero is called a non-degenerate basic solution.
 - (d) The basic feasible solution which maximizes or minimizes the objective function is called an optimum basic feasible solution.
- Which of the following is not correct?
 - (a) Simplex method is an iterative process which involves the substitution of variables for obtaining successively better solutions.
 - ☒ (b) Solution by Simplex method requires that an LPP should have at least one non-negative values in the right hand side of the constraints.
 - (c) For solving an LPP by Simplex method, it is essential that all variables involved are non-negative.
 - (d) Simplex method requires that all the constraints should be first converted into equations.
- For maximization linear programming problem, the simplex method is terminated when all the net-evaluations are
 - (a) negative,
 - ☒ (b) non-negative,
 - (c) zero,
 - (d) non-positive.
- A necessary and sufficient condition for a basic feasible solution to a minimization LPP to be an optimum is that (for all j):
 - (a) $z_j - c_j \geq 0$,
 - ☒ (b) $z_j - c_j \leq 0$,
 - (c) $z_j - c_j = 0$,
 - (d) $z_j - c_j > 0$ or $z_j - c_j < 0$.
- At any iteration of the usual Simplex method, if there is at least one basic variable in the basis at zero level and all $(z_j - c_j) \geq 0$, the current solution is
 - (a) Infeasible,
 - (b) Unbounded,
 - (c) Non-degenerate,
 - ☒ (d) Degenerate.

LINEAR PROGRAMMING—SIMPLEX METHOD

7. The role of artificial variables in simplex method is
 - ☒ (a) to aid in finding initial basic feasible solution.
 - (b) to start phases of simplex method.
 - (c) to find shadow prices from the final simplex table.
 - (d) none of the above.
8. For maximization LPP, the objective function coefficient for an artificial variable is
 - (a) $+M$,
 - ☒ (b) $-M$,
 - (c) $+1$,
 - (d) zero.
9. In a maximization LPP, if at least one artificial variable is in the basis, but not at zero level and the coefficient of M in each of the net evaluation ($z_j - c_j$) is non-negative, then we have
 - (a) a feasible solution,
 - (b) no feasible solution
 - (c) an unbounded solution,
 - (d) an optimum solution.
10. In final (optimum) simplex table, if $z_j - c_j = 0$ for at least one non-basic variable, then there will be
 - (a) an unbounded solution,
 - (b) infeasible solution,
 - ☒ (c) alternative solution,
 - (d) cycling.
11. If a negative value appears in the solution values (x_B) column of the simplex method, then
 - (a) the basic solution is optimum,
 - ☒ (b) the basic solution is infeasible,
 - (c) the basic solution is unbounded,
 - (d) all of the above.
12. If an optimum solution is degenerate, then
 - (a) the solution is infeasible,
 - (b) there are alternative optimum solutions.
 - ☒ (c) the solution is of no use to the decision maker.
 - (d) none of the above.
13. Which of the following is not correct?
 - (a) Degeneracy in an LPP may arise at the initial stage.
 - ☒ (b) A degenerate solution can never be optimum.
 - (c) Degeneracy may be a temporary phenomenon.
 - (d) The Big-M method and the Two-Phase method do not require the same number of iterations for solving an LPP.
14. When we solve a system of simultaneous linear equations by using *Two-Phase Simplex Method*, the values of decision variables may be
 - (a) positive,
 - (b) negative,
 - (c) zero,
 - ☒ (d) positive and/or negative.
15. Which of the following is not correct?
 - (a) An LPP may have no optimum solution, a unique and optimum solution, multiple optimum solution, or an unbounded solution.
 - (b) In the optimum solution to an LPP if a basic variable is zero, then multiple optimum solutions are indicated.
 - (c) Multiple optimum solutions to an LPP would all have the same objective function values and would consume the same amount of the resources.
 - (d) The inverse of a square matrix can be obtained by using *Simplex method*.
16. In the context of LPP, which of the following is not correct?
 - (a) When the constraints are of ' $\geq$ ' type, surplus variables are introduced to convert them into equations.
 - (b) Artificial variables are no tangible relationship with the decision variables.
 - ☒ (c) Surplus variables cannot appear in the basis of the optimum solution to an LPP.
 - (d) An artificial variable can be dropped for further calculations once it becomes non-basic or gets removed at any stage.

ANSWERS

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|---------|---------|---------|---------|---------|
| 1. (a) | 2. (c) | 3. (b) | 4. (b) | 5. (b) |
| 6. (d) | 7. (a) | 8. (b) | 9. (b) | 10. (c) |
| 11. (b) | 12. (c) | 13. (b) | 14. (d) | 15. (b) |
| 16. (c) | | | | |